

Millimeter imaging of HD 163296: probing the disk structure and kinematics^{*}

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ABSTRACT

We present new multi-wavelength millimeter interferometric observations of the Herbig Ae star HD 163296 obtained with the IRAM/PBI, SMA and VLA arrays both in continuum and in the ^{12}CO , ^{13}CO and C^{18}O emission lines. Gas and dust properties have been obtained comparing the observations with self-consistent disk models for the dust and CO emission. The circumstellar disk is resolved both in the continuum and in CO. We find strong evidence that the circumstellar material is in Keplerian rotation around a central star of $2.6 M_{\odot}$. The disk inclination with respect to the line of sight is $46^{\circ} \pm 4^{\circ}$ with a position angle of $128^{\circ} \pm 4^{\circ}$. The slope of the dust opacity measured between 0.87 and 7 mm ($\beta = 1$) confirms the presence of mm/cm-size grains in the disk midplane. The dust continuum emission is asymmetric and confined inside a radius of 200 AU while the CO emission extends up to 540 AU. The comparison between dust and CO temperature indicates that CO is present only in the disk interior. Finally, we obtain an increasing depletion of CO isotopomers from ^{12}CO to ^{13}CO and C^{18}O . We argue that these results support the idea that the disk of HD 163296 is strongly evolved. In particular, we suggest that there is a strong depletion of dust relative to gas outside 200 AU; this may be due to the inward migration of large bodies that form in the outer disk or to clearing of a large gap in the dust distribution by a low mass companion.

1. Introduction

Millimeter and sub-millimeter interferometers are providing an increasingly detailed description of disks around pre-main sequence stars of solar (T Tauri stars; TTS) and intermediate mass (Herbig Ae; HAe). Both dust continuum emission and emission in molecular lines are observed and spatially resolved in a number of disks, yielding information on the disk density and temperature, the dust properties and the gas chemistry and dynamics in the

outer disk (e.g., Natta et al. 2007, Dutrey et al. 2006, and references therein). Thanks to the recent instrumental improvements, it is now possible to build upon the original detections and study more accurately the disk structure details. The number of well-studied disks is however still very small, practically restricted to the most massive and luminous ones; still, it is clear that disks differ from one another. Recently, it has been reported evidence of spiral structures in AB Aur, a 2-3 Myr old intermediate mass star, and of deviations from Keplerian rotation (Piétu et al. 2005; Corder et al. 2005); the classical TTS LkCa15 has a large inner hole of size ~ 50 AU depleted of dust, while the HAe star MWC 480 has a smooth disk with an optically thick (at millimeter wavelengths) inner region of radius ~ 35 AU (Piétu et al. 2006). Both spiral structures and large gaps are evidence of dynamical perturbations, possibly due to the effect of large planets. The existence of both unperturbed and distorted disks among pre-main sequence stars suggests that the planet formation is actively occurring during this evolutionary stage, leaving detectable marks on the parent disks. It is therefore important to study in detail as many disks as possible,

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in order to characterize their basic properties and to detect deviations from the simple patterns of homogeneous disks in Keplerian rotation.

We report in this paper a detailed study of the disk associated to the H Ae star HD 163296, using observations in the continuum and CO lines obtained with three different interferometers, namely the Very Large Array (VLA) at 7 mm, IRAM Plateau de Bure Interferometer (PBI) at 1.3 and 2.6 mm and the Submillimeter Array (SMA) at 0.87 mm. HD 163296 is a star of spectral type A1, mass of roughly $2.3 M_{\odot}$, distance 122 pc (van den Ancker et al. 1998). Early OVRO observations (Mannings and Sargent 1997) have shown the presence of a disk with a minimum mass $\sim 0.03 M_{\odot}$ and evidence of rotation from the CO lines. The disk is seen in scattered light by Grady et al. (2000, 1999), with radius of ~ 500 AU; it has an associated jet seen in Ly- α with HST, extending on both sides of the disk orthogonally to it (Devine et al. 2000, Wassell et al. 2006). Natta et al. (2004) found evidence of evolved dust in the outer disk of HD 163296 by comparing the VLA 7 mm flux to the OVRO observations.

The results we present here have much higher spatial resolution and wavelength coverage than what has been previously reported. They allow us to measure accurately the dynamics of the disk as well as the disk and dust properties and to test the capability of disk models to account for the observations. As we will show, they suggest that the HD 163296 system is probably evolving towards a debris disk phase.

The structure of the paper is as follows. Sec. 2 will describe the observations. The results will be presented in Sec. 3, where we will derive some of the disk parameters. A more detailed analysis, using self-consistent disk models of the dust and CO line emission will be presented in Sec. 4; Sec. 5 contains the results, which will be further discussed in Sec. 6. Summary and conclusions follow in Sec. 7 and 8.

2. Observations and data reduction

2.1. PBI observations

The PBI observations were carried over the 2003/2004 winter season. The six 15 m dishes were used in the most extended configuration providing a baseline coverage between 25 and 400 m. The corresponding angular resolutions are reported in Tab. 1. The receivers were tuned to observe the ^{12}CO J=2–1 line and the nearby continuum at 1.3 mm, while at 2.8 mm the ^{13}CO J=1–0, and C^{18}O J=1–0 lines were observed along with the continuum. Bandpass and complex gain calibrations were ensured by observations of standard IRAM calibrators. The phase stability was excellent during our observations and only a minimal amount of editing of the data was necessary. All calibrations were performed using the standard CLIC suite of programmes within the GILDAS software package. The calibrated uv data were then exported for the subsequent

analysis. The accuracy of the flux density scale calibration is expected to be within 20% at these wavelengths.

2.2. SMA observations

The SMA observations of HD 163296 were made on August 23rd, 2005 using the Compact Configuration of seven of the 6 meter diameter antennas, which provided 21 independent baselines ranging in length from 8 to 80 meters. The SMA digital correlator was configured with a narrow band of 512 channels over 104 MHz, which provided 0.2 MHz frequency resolution, or 0.18 km s^{-1} velocity resolution at 345 GHz, and the full correlator bandwidth was 2 GHz. The weather was good with $\tau(225 \text{ GHz})$ around 0.06 and the double-sideband (DSB) system temperature were between 200 and 500 K. The source HD 163296 was observed from HA -3 to 4.5. Calibration of the visibility phases and amplitudes was achieved with observations of the quasar 1921-293, typically at intervals of 25 minutes. Observations of Uranus provided the absolute scale for the flux density calibration and the uncertainties in the flux scale are estimated to be 20%. The data were calibrated using the MIR software package¹.

2.3. VLA observations

HD 163296 was observed at the NRAO/VLA as part of a larger survey for 7 mm disk emission around Herbig Ae stars (see Natta et al., 2004). Data were obtained with the array in the C and D configurations, in several occasions from Dec 2001 through May 2003. Accurate pointing was ensured by hourly pointing sessions at 3.6 cm on a bright extra galactic object. The array offered baselines from the shadowing limit through ~ 3.4 km, although some data was obtained in a hybrid DnA configuration, all the data from the longer baselines had to be rejected due to large phase fluctuations that could not be corrected. The resulting uv-plane coverage offered an angular resolution of $0.5''$ and a maximum recoverable size of the order of $\sim 40''$. All the data was edited and calibrated using standard recipes in AIPS. The short term complex gain variations were corrected using frequent (few minutes cycle) observations of the quasar 1820–254, while the flux scale was set observing the VLA calibrator 1331+305. This procedure is expected to be accurate within $\sim 15\%$ at 7 mm.

3. Observational results

The continuum maps obtained at 0.87 mm, 1.3 mm, 2.8 mm and 7 mm are shown in Fig. 1. Channel maps, integrated intensity and mean velocity maps of the ^{12}CO J=2–1, ^{13}CO J=1–0 and ^{12}CO J=3–2 transitions are shown in Fig. 2, 3 and 4 respectively. At the wavelength corresponding to the C^{18}O J=1–0 transition we did not detect any emission; the continuum integrated fluxes are reported in Tab. 1.

¹ <http://cfa-www.harvard.edu/cqi/mircook.html>

| λ (mm) | beam FWHM | PA | emission FWHM | flux (mJy) |
|-------------------|------------------------|-------------|------------------------|----------------|
| 0.87 | $3''.14 \times 2''.21$ | 20° | $3''.60 \times 2''.64$ | 1910 ± 20 |
| 1.3 | $1''.95 \times 0''.42$ | 7° | $2''.01 \times 0''.83$ | 705 ± 12 |
| 2.8 | $3''.3 \times 0''.94$ | 8° | $3''.5 \times 1''.4$ | 77.0 ± 2.2 |
| 7 | $1''.71 \times 0''.81$ | 172° | $1''.71 \times 0''.94$ | 4.5 ± 0.5 |

Table 1. Column 2 and 3 show the size and the position angle of the synthesized beam of the HD 163296 observations performed with SMA (at 0.87 mm), PBI (at 1.3 mm and 2.7 mm) and VLA (at 7 mm). Column 4 shows the FWHM size of the detected emission along the major and minor axis of the beam. Column 5 shows the integrated flux with the uncertainties due to the statistical errors.

With simple physical assumptions, these observations allow us to determine some fundamental parameters of the star+disk system as the stellar and the disk masses, the contribution to the observed fluxes of free-free gas emission, the wavelength dependence of the observed flux at millimeter wavelengths and the related dust grain opacity.

3.1. Disk morphology and apparent size

The $12'' \times 12''$ continuum maps of HD 163296 are shown in Fig. 1. At all wavelengths, the peak is coincident with the position of the optical star as measured from Hipparcos and, given the respective synthesized beams FWHM (see Tab. 1), the emission is resolved and elongated approximately in the east-west direction. Approximating the source with a circularly symmetric geometrically thin disk and taking into account the beam shape, the observed aspect ratio of the level contours implies an inclination of the disk plane from the line of sight of $45^\circ \pm 20^\circ$ and a position angle of $120^\circ \pm 30^\circ$, in rough agreement with the values obtained by Mannings and Sargent (1997) using marginally resolved OVRO observations (58° and 126° respectively).

The emission is resolved at all the wavelengths in the East-West direction. The fainter contour levels are not centrally symmetric, showing excess emission in the east half of the image, better visible in the 0.87 and 1.3 mm maps. Both the disk size and the morphology will be discussed in more detail in Sec. 6.

3.2. Disk kinematics

As shown in Fig. 2, 4 and 3, in all the detected molecular line transitions, the emission is resolved, showing a velocity pattern typical of an inclined rotating disk characterized by a position angle of about 130° (a more precise estimate of the position angle will be presented in Sec. 5). The velocity-position diagram calculated along this direction (see Fig. 5) shows a well defined “butterfly shape” typical of Keplerian rotation. A first estimate of the mass of the central object and of the dimension of the disk can

be obtained by comparing the observed velocities with the Keplerian law:

$$v_\epsilon = C \cdot \epsilon^{-1/2}, \quad (1)$$

where ϵ is the angular distance from the central star and v_ϵ is the component of the disk rotational velocity along the line of sight. If the stellar mass M_\star is in solar units, the stellar distance d in parsec and θ is the disk inclination ($\theta = 0$ means pole-on disk), the constant $C \simeq 30\sqrt{M_\star/d} \sin \theta$ is the component along the line of sight of the disk rotational velocity (in km/sec) at $\epsilon = 1''$. As shown in Fig. 5 the envelopes of both the ^{12}CO and ^{13}CO emissions are in agreement with $C \simeq 2.7 \pm 0.4$ km/sec. This value corresponds to a stellar mass of $2.0 \pm 0.5 M_\odot$ for an inclination of 45° and $d = 122$ pc. Note finally that the disk rotation is clearly observed at least up to a distance of about $4''$, corresponding to a minimum disk outer radius of about 500 AU. We will discuss in more detail the determination of the stellar mass and the disk outer radius in Sec. 5, using a detailed model for the continuum and CO molecular emission.

3.3. Free-free contribution and spectral index

The continuum spatially integrated fluxes of HD 163296 and the corresponding spectral energy distribution are given in Tab. 1 and shown in Fig. 6, respectively. In addition to our measurements (full squares), observations at 0.7, 1.3, 3.6 and 6.1 mm are from Natta et al. (2004 and references therein) while observations at 0.75, 0.8, 0.85, 1.1 and 1.3 mm are from Mannings (1994).

Assuming that the observed flux at 3.6 and 6.1 cm is dominated by free-free emission from a wind (with a spectral index of 0.6), the free-free contribution at 7 mm corresponds to 1.2 mJy (27% of the observed flux), while it is negligible at shorter wavelengths.

After the subtraction of the free-free component, the millimeter spectral index α_{mm} ($F_\lambda \propto \lambda^{-\alpha_{mm}}$) calculated between 1 mm and 7 mm is 3.0 ± 0.1 , slightly higher than the value $\alpha_{mm} = 2.6 \pm 0.2$ obtained by Natta et al. (2004) using VLA and OVRO fluxes only.

3.4. Disk mass

Assuming that the dust emission is optically thin at millimeter wavelengths and that the dust is isothermal, the measured flux can be used to estimate the product of the disk total mass M times the dust opacity k_ν , through the relation:

$$M \cdot k_\nu = \frac{F_\nu d^2}{B_\nu(T)}, \quad (2)$$

where d is the source distance and T is the temperature of the emitting dust. At millimeter wavelengths, the dust opacity can be parametrized by a power law

$$k = 0.01 \cdot (\lambda/1.3\text{mm})^{-\beta} \text{cm}^2 \text{g}^{-1}, \quad (3)$$

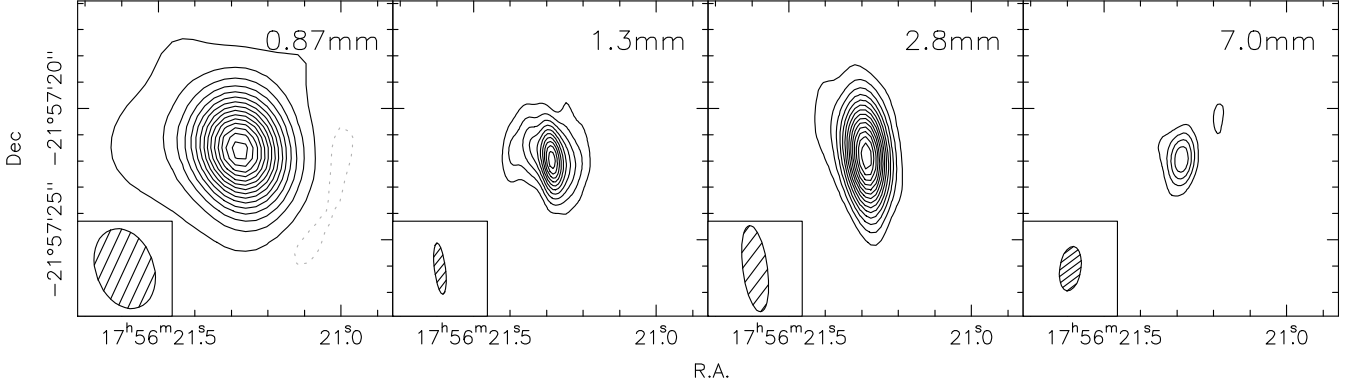


Fig. 1. Continuum maps of HD 163296 at 0.87, 1.3, 2.8 and 7 mm, starting from the left. In order to highlight the extended morphology of the disk, the first contour level in the 0.87 mm map corresponds to 30 mJy (3σ), the second to 6σ while the inner contour levels are spaced by 10σ . At longer wavelength the contour levels are all spaced by 3σ , corresponding to 12 mJy at 1.3 mm, 3.3 mJy at 2.8 mm and 0.75 mJy at 7 mm. The small boxes show the relative synthesized beams. The integrated fluxes, the beam dimensions and orientations are summarized in Tab. 1

where the normalization at $\lambda = 1.3 \text{ mm}$ assumes a dust/gas mass ratio of 0.01 (Beckwith et al., 1990, 1991). Taking a characteristic temperature for the dust in the outer disk of an early A star of 30 K (Natta et al. 2000), we derive a total gas+dust mass of $0.12 M_{\odot}$ for the circumstellar material in HD 163296. This rough mass determination, that does not take into account the presence of optically thick emission from the inner part of the disk, nor of temperature gradients, will be discussed in more detail in Sec. 5.2.

With these simplifying assumptions, the slope of the dust opacity is $\beta = \alpha - 2 \sim 1$, where α is the spectral index obtained in the previous section.

4. Disk Models

The disk parameters derived in Sec. 3 under a number of very crude assumptions can only provide order-of-magnitude estimates. A more quantitative analysis requires to compare the observations to more sophisticated model predictions. We chose to perform the comparison using the observed visibilities (rather than reconstructed images), following a similar approach as the one discussed by Dutrey et al. (2006).

This method requires to decide “a priori” which family of models is likely to describe the observed object. In view of the results described in Sec. 3, we model the millimeter emission of HD 163296 (continuum and CO lines) as coming from a circumstellar disk. We assume that the disk is heated by the stellar radiation only, and that any viscous contribution can be neglected. This is very likely a good approximation, given the relatively low accretion rate measured in HD 163296 ($\sim 10^{-7} M_{\odot}/\text{yr}$; Garcia Lopez et al., 2006).

The disk structure and emission is computed using the 2-layer approximation of Chiang and Goldreich (1997), as developed by Dullemond et al. (2001). Similar models have

been used in Testi et al. (2003) and Natta et al. (2004), to analyze the (sub)millimeter emission of a number of Herbig Ae stars. We refer to these papers for a more detailed description.

The inner disk is characterized by the presence of a *puffed-up* inner rim located at the dust evaporation radius (Isella and Natta, 2005). The combined rim+disk flux is calculated taking into account the shadow that the rim casts over the outer disk.

The disk geometry can be fully flared, as in hydrostatic equilibrium disks where gas and dust are well mixed. If dust growth and settling are important, the flaring angle decreases: the resulting radial temperature profile is flatter, affecting the SED in the mid and far infrared (D’Alessio et al. 2006 and references therein). As shown in Fig. 6, the SED of HD 163296 is well reproduced by a fully flared disk model. The fit of the SED becomes very poor if the flaring angle is reduced by more than a factor of two, which corresponds to a small variation on temperature radial profile.

Once the stellar properties are known, the disk structure is completely characterized by the following parameters: the disk mass (M_d), the disk outer radius (R_{out}), the dependence of the surface density on radius ($\Sigma \propto r^{-p}$) and the properties of dust on the disk surface and midplane. In addition, the observed emission depends on the orientation of the disk with respect to the observer, which is characterized by the inclination i of the disk with respect to the line of sight ($i = 0$ for face-on disks) and the position angle PA .

4.1. Continuum emission

The continuum emission at millimeter and sub-millimeter wavelengths is computed by ray integration as in Dullemond et al. (2001). We describe the midplane dust opacity at long wavelengths as a power law of index β ,

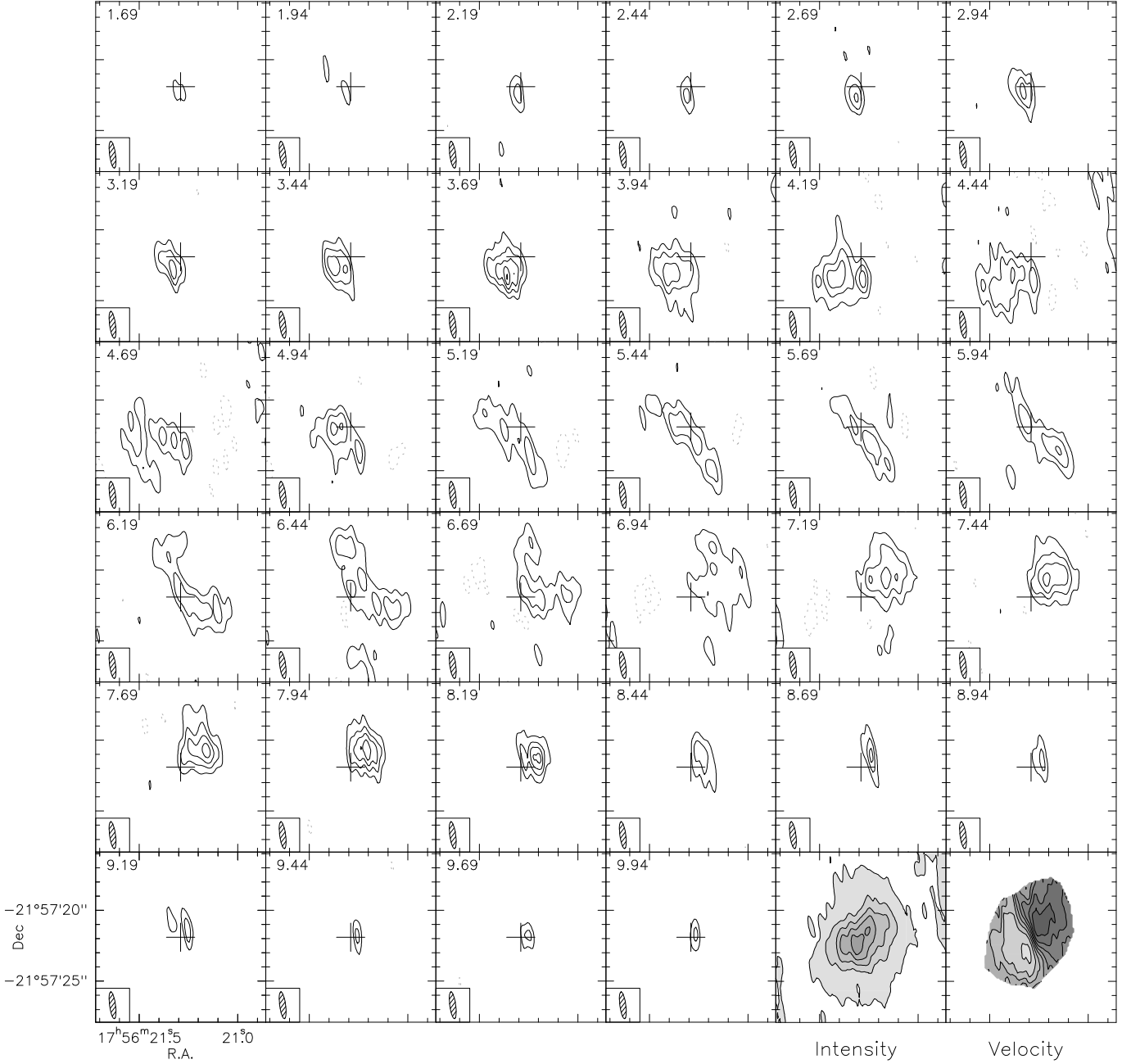


Fig. 2. Velocity channel maps of the ^{12}CO J=2–1 emission. The velocity resolution is 0.25 km/sec. The LSR velocity is indicated in the upper left corner of each panel. The angular resolution (synthesized beam), indicated in the small boxes, is $1.95'' \times 0.42''$ at PA 7° ; the contour spacing is 0.23 Jy/beam corresponding to 3σ . The last two panels show the integrated intensity (contour levels spaced by 0.4 Jy/beam km s^{-1}) and the velocity field (contour levels from 3 km s^{-1} to 9 km s^{-1} spaced by 0.5 km s^{-1}) respectively.

with β a free parameter, as in Eq. 3. At short wavelengths and in the disk surface we adopt the dust opacity of astronomical silicates (Weingartner and Draine, 2001). The inner disk radius is the dust sublimation radius, as in the rim models of Isella et al. (2006) for large ($\sim 1\mu\text{m}$) grains, and it is equal to 0.45 AU; the dust on the disk surface is as in Natta et al. (2004). Neither of these two quantities is relevant for the following analysis.

4.2. CO emission

The observed CO emission originates in the outer layers of the disk, at heights that depend on the optical depth of the specific transition. Once the disk structure is specified, as described above, one needs to compute, at each radius, the gas temperature profile in the vertical direction. This is a complex problem, whose results depend on a number of not well known properties, among them the X-ray

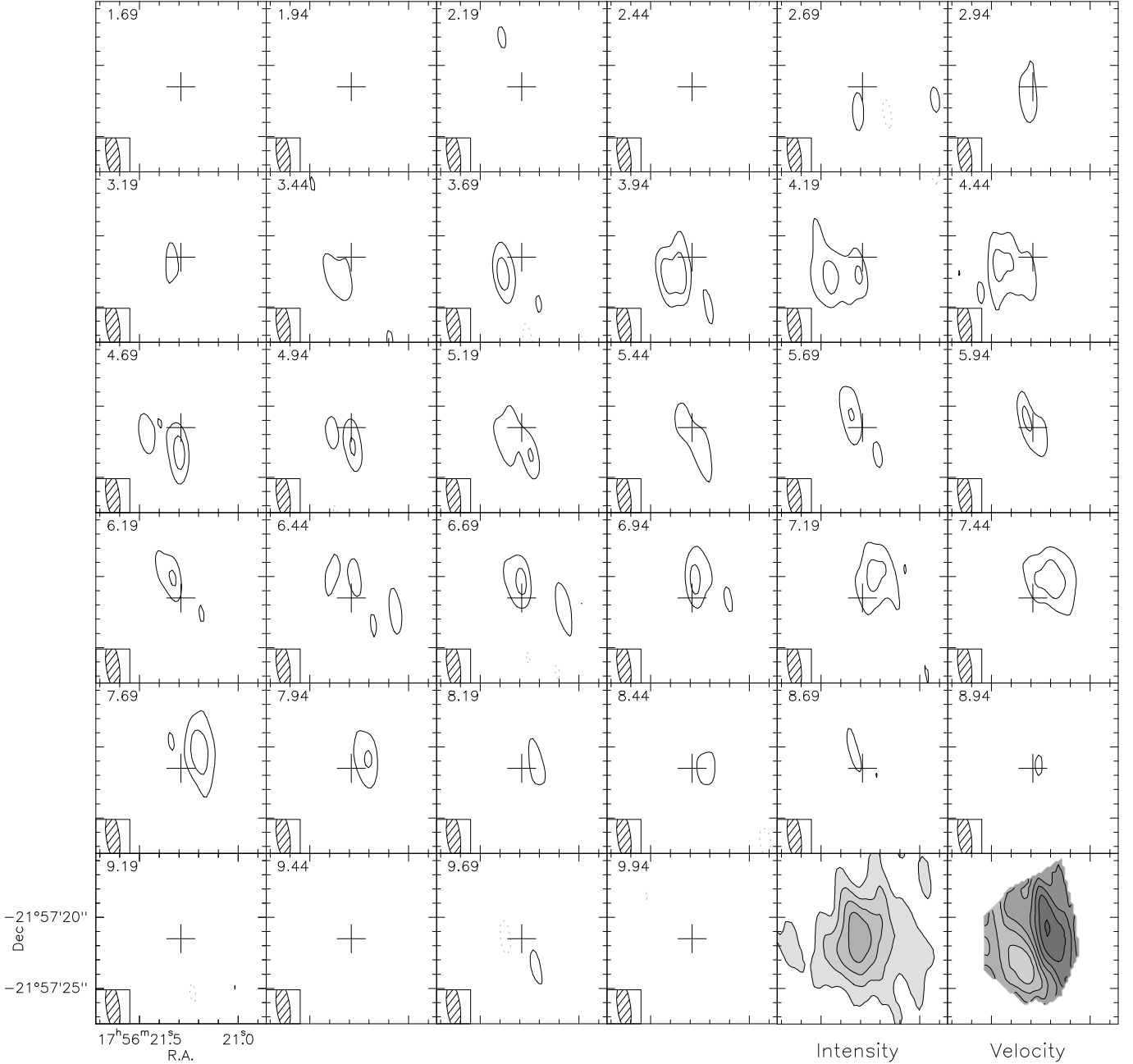


Fig. 3. Velocity channel maps of the ^{13}CO $J=1-0$ emission. The velocity resolution is 0.25 km/sec. The LSR velocity (km s^{-1}) is indicated in the upper left corner of each panel. The angular resolution (synthesized beam), indicated in the small boxes, is $3.3'' \times 0.94''$ at PA 8° ; the contour spacing is 0.09 Jy/beam corresponding to 3σ . The last two panels show the integrated intensity (contour levels spaced by 0.12 Jy/beam) and the velocity field (contour levels from 3 km s^{-1} to 9 km s^{-1} spaced by 0.5 km s^{-1}) respectively.

field and the role of very small grains in heating the gas (e.g., Dullemond et al. 2006). Therefore, we use a parametric description assuming that for each CO transition the excitation temperature is the same at all z and can be described as a power-law of r in the form:

$$T_{\text{line}} = T_{\text{line}}(r_0)(r/r_0)^{-q}. \quad (4)$$

The assumption of a constant excitation temperature along the vertical direction is correct for optically thick

lines, and/or if the velocity gradient along the line of sight is very large. In both cases, the contribution at each wavelength from the line of sight under consideration comes from a small region only, where the optical depth in the line is of order unity. For any CO line, the height to which $T_{\text{line}}(r)$ refers is therefore different, depending on the density and velocity structure, as well as on the disk inclination angle. The values of $T_{\text{line}}(r_0)$ and q for each CO transition are free parameters. A similar procedure has been

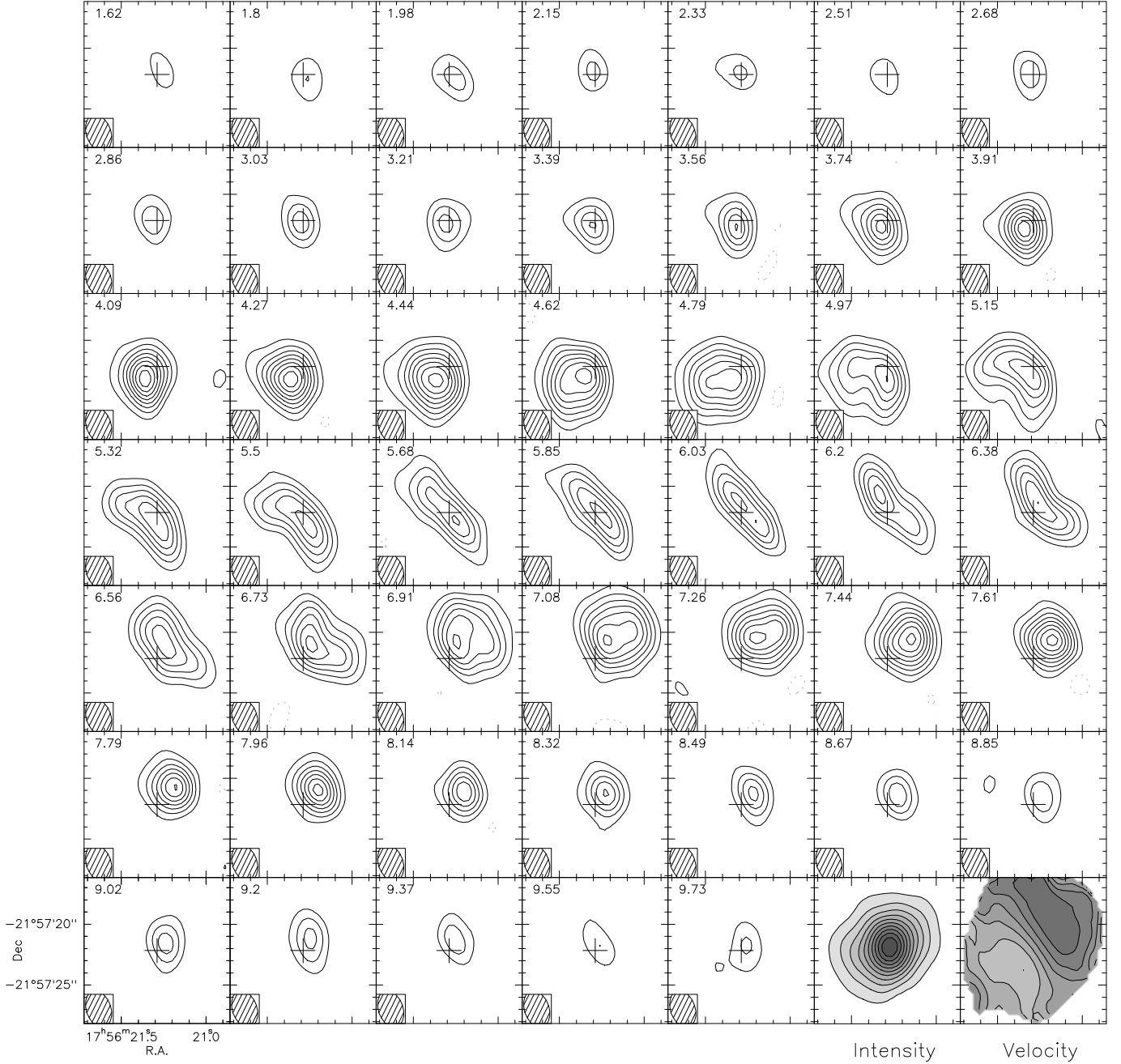


Fig. 4. Velocity channel maps of the ^{12}CO $J=3-2$ emission. The velocity resolution is 0.18 km/sec. The LSR velocity (km s^{-1}) is indicated in the upper left corner of each panel. The angular resolution (synthesized beam), indicated in the small boxes, is $3.4'' \times 2.21''$ at PA 20° ; the contour spacing is 1.5 Jy/beam corresponding to 3σ . The last two panels show the integrated intensity (contour levels spaced by 5 Jy/beam km s^{-1}) and the velocity field (contour levels from 3 km s^{-1} to 9 km s^{-1} spaced by 0.5 km s^{-1}) respectively.

used by Dutrey et al. (1994) and Dartois et al. (2003) in their study of the CO emission of T Tauri disks.

In the analysis of CO observations we have assumed $^{12}\text{CO}/\text{H}_2 = 7.0 \cdot 10^{-5}$, $^{13}\text{CO}/\text{H}_2 = 1.0 \cdot 10^{-6}$ and $\text{C}^{18}\text{O}/\text{H}_2 = 1.3 \cdot 10^{-7}$, which correspond to an isotopic ratio $^{12}\text{CO}/^{13}\text{CO} = 70$, $^{12}\text{CO}/\text{C}^{18}\text{O} = 550$ (Beckwith and Sargent, 1993; Dutrey et al., 1996; and reference therein)

As described in detail in the Appendix, we have developed a code which computes, for each CO transition, the line intensity and profile as function of the disk parameters, namely the inclination and PA, the density and temperature profile, the disk outer radius. In addition, we assume that the disk is in Keplerian rotation around the central star and vary the stellar mass independently for each line.

| Parameters | Continuum | ^{12}CO J=2-1 | ^{12}CO J=3-2 | ^{13}CO J=1-0 |
|--------------------------------------------|--------------------------|-------------------------|--------------------------|-------------------------|
| M_* (M_\odot) | 2.6^a | $2.6^{+0.3}_{-0.5}$ | 2.4 ± 0.8 | 2.6 ± 0.6 |
| PA | $120^\circ \pm 20^\circ$ | $128^\circ \pm 5^\circ$ | $130^\circ \pm 13^\circ$ | $130^\circ \pm 8^\circ$ |
| $Incl$ | $40^\circ \pm 12^\circ$ | $45^\circ \pm 5^\circ$ | $45^\circ \pm 10^\circ$ | $50^\circ \pm 8^\circ$ |
| R_{out} (AU) | 200 ± 15 | 550 ± 50 | 550 ± 100 | 500 ± 80 |
| Σ_{10AU} (g/cm^2) | 46 ± 4 | 90 ± 70 | 90^a | 4^{+12}_{-3} |
| p | 0.8 ± 0.1 | $0.6^{+0.3}_{-0.1}$ | 0.6^a | 1.0 ± 0.5 |
| $T_{CO,100AU}$ (K) | | 40^{+2}_{-5} | 60 ± 20 | 30 ± 10 |
| q | | $0.5^{+0.2}_{-0.1}$ | 0.8 ± 0.4 | 0.8 ± 0.4 |
| β | 1.0 ± 0.1 | 1.0^a | 1.0^a | 1.0^a |
| χ^2_r | 2.6 | 1.17 | 1.05 | 1.15 |

Table 2. Parameters of the disk structure relative to the best fit models for the continuum and the CO emissions as described in Sec. 5. For each parameters uncertainties are given at 1σ level. ^a Fixed parameter.

In the following, we assume a gas turbulence velocity $v_{turb} = 0$ km/sec. Note that for v_{turb} in the range observed in other TTS and H Ae (0.07-0.38 km/sec from Piétu et al. 2007, 2005, 2003; Dutrey et al. 1994, 1996; Dartois et al. 2003; Simon et al. 2001) the results does not change. This is due to the fact that, for the inclination of the HD 163296 disk, the CO lines width is dominated by the differential disk rotation.

5. Results

5.1. Method of analysis

The observations of HD 163296 have been analyzed by comparing the observed and the model predicted complex visibilities. For each set of data, the best fit model has been obtained minimizing the $\chi^2 = \sum_i ((Re_{mod,i} - Re_{obs,i})^2 + (Im_{mod,i} - Im_{obs,i})^2) \cdot W_i$, where Re_X and Im_X are the real and the imaginary part of the complex visibility measured (*obs*) and predicted (*mod*) in the point i of the uv-plane, and W_i is the weight of each measure. For each CO transition, the χ^2 has been computed by the simultaneous fitting of 14 velocity channels chosen in order to optimize the sampling of the line profile. The χ^2 minimization has been performed exploring a wide region of the space of model parameters. For each parameter, the 1σ uncertainties are estimated as $\chi^2_{1\sigma} = \chi^2_m + \sqrt{2n}$, where n is the number of degrees of freedom and χ^2_m is the χ^2 value of best fit model.

5.2. Continuum emission

The continuum data at the four observed wavelengths (0.87, 1.3, 2.7, 7 mm) have been analyzed independently to estimate the best disk parameters and their uncertainties. We have varied the two parameters which define the position of the disk on the plane of the sky, namely the inclination and position angle, as well as the three physical parameters which affect the continuum dust emission, namely the disk outer radius R_{out} , the slope p of the sur-

face density profile and the product $\Sigma_{10AU} \times k_\lambda$. Since the continuum emission has a very weak dependence on the mass of the central star, we fixed $M_* = 2.6 M_\odot$ (see Sec. 5.3).

The values of the parameters obtained at different wavelengths are the same within the uncertainties. In column 1 of Tab. 2 we show the values of the resulting best fit model obtained by combining the independent results at the four different wavelengths. The parameters constraint is dominated by the 1.3 mm data, which have the best sensitivity and resolution.

The surface density radial profile has a slope $p = 0.81 \pm 0.01$ and the disk outer radius is $R_{out} = 200 \pm 15$ AU. The very good constraints on both parameters is due to the favorable orientation of the beam at 1.3 mm with the maximum resolution ($0.42''$) in almost the same direction of the major axis of the disk. Note that the formal error on p is extremely low. On the other hand, small variations on the disk flaring (that allow to fit the SED) lead to correspondingly small variation of the disk radial temperature profile and on the value of p . Taking into account this fact, ± 0.1 is a more reasonable uncertainty for p . The formal uncertainties on the other parameters are much larger than those introduced by small variations of the flaring angle.

The four values of $\Sigma_{10AU} \times k_\lambda$ are used to constrain the slope β of the dust opacity law (see Eq. 3) between 0.87 and 7 mm, which turns out to be 1.0 ± 0.1 . This confirms the presence of large grains in the HD 163296 circumstellar disk (Natta et al. 2004). Note that the optically thick disk region at 1.3 mm has size of ~ 6 AU and contributes only 4% of the observed flux, so that β is very similar to that derived in Sec. 3.3. The observations constrain only the dependence of the dust opacity on wavelength, not its absolute value. The value of Σ_{10AU} given in Tab. 2 is obtained from $\Sigma_{10AU} \times k_{1.3\text{mm}}$ assuming $k_{1.3\text{mm}} = 0.01 \text{ cm}^2/\text{g}$.

The residuals for each wavelength are shown in Fig. 7. They have been reconstructed from the residuals in the uv-

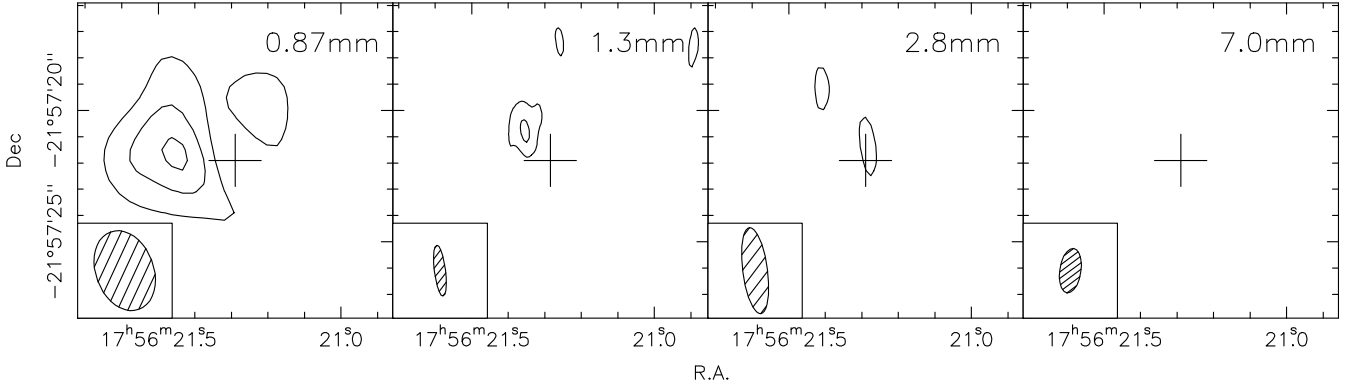


Fig. 7. Maps of the residuals relative to the best fit model for the continuum emission (see Fig. 1 for the observations). The contour level are spaced by 3σ corresponding to 30 mJy at 0.87 mm, 12 mJy at 1.3 mm, 3.3 mJy at 2.8 mm and 0.75 mJy at 7 mm. The small boxes show the relative synthesized beams.

plane with the same procedure used to obtain the images in Fig. 1. Residual contours are generally lower than 3σ with the exception of the 0.87 and 1.3 mm maps, where a flux asymmetry in the east half of the map (see also Sec. 3.1) is clearly visible. This structure, not detected at longer wavelengths, requires more resolved observations to be investigated in detail.

5.3. CO emission

The analysis of the CO emission has been carried out separately for the different CO transitions and the corresponding best fit parameters are given in Tab. 2.

The observed ^{12}CO J=2-1 emission is well fitted by a Keplerian disk orbiting a central star with mass $M_\star = 2.6^{+0.3}_{-0.5} M_\odot$. Fig. 8 shows the position-velocity residuals obtained subtracting the best fit model from the observed uv-table: no evidence of non-Keplerian rotation or stellar outflow is detected, within the actual instrumental sensitivity. Both the position angle and the inclination are in agreement with the values obtained from the continuum. Since the line is optically thick, the constraint on the gas surface density is poor. The inferred outer radius of the disk is 550 ± 50 AU, more than two times larger than the value obtained from the continuum and similar to the result obtained by Thi et al. (2004) from the model fitting of single dish line profiles. The radial temperature profile of the ^{12}CO has a slope $q = 0.5^{+0.2}_{-0.1}$ and a value of 40^{+2}_{-5} K at 100 AU.

Since the ^{12}CO J=3-2 line is optically thick and given the relatively low resolution of the SMA observations, the measurements do not constrain the CO radial density profile. In this case we fix both p and $\Sigma_{10\text{AU}}$ equal to the values obtained for the ^{12}CO J=2-1 and vary the other parameters. The results for the inclination, position angle, disk outer radius and CO temperature are in good agreement with the values obtained for the ^{12}CO J=2-1, with larger uncertainties due to the lower spatial resolution.

Finally, the model fit to the ^{13}CO J=1-0 line gives results consistent with those obtained from the ^{12}CO lines

with the exception of the value of $\Sigma_{10\text{AU}}$ which is significantly smaller. This discrepancy may be due to a depletion of the ^{13}CO and will be discussed in Sec. 6.5. The radial temperature profile of the ^{13}CO has a slope $q = 0.8 \pm 0.4$ and a value of 30 ± 10 K at 100 AU. We will comment on the gas physical conditions in Sec. 6.5. In general, the parameter constraints obtained from the ^{13}CO are not so good as those obtained for the ^{12}CO J=2-1, as expected given the lower resolution of the observations.

6. Discussion

6.1. Disk orientation

The disk orientation is well determined by our set of measurements: it has a moderate inclination with respect to the line of sight (the mean of the inclination values is $46^\circ \pm 4^\circ$) with a position angle of $128^\circ \pm 4^\circ$.

6.2. Disk kinematics and stellar mass

All the observations are consistent with the emission of a circumstellar disk in Keplerian rotation around a star of $2.6 M_\odot$, assuming the Hipparcos distance of 122^{+17}_{-13} pc (van den Ancker et al. 1998). Within the error, the stellar mass is in agreement with the value of $2.3 M_\odot$ (Natta et al., 2004) obtained from the location of the star on the HR diagram, using Palla and Stahler (1993) evolutionary tracks; the corresponding stellar age is of about 5 Myr.

6.3. Disk outer radius

The model fitting (Tab. 2) shows that the value of the disk outer radius inferred from the continuum dust emission (200 ± 15 AU) is almost three times smaller than the value obtained from the CO analysis (where 540 ± 40 AU is the mean value). Since our method takes into account the sensitivity limits of the different interferometric observations, this discrepancy can not be explained by the fact that the disk outer regions have a continuum surface

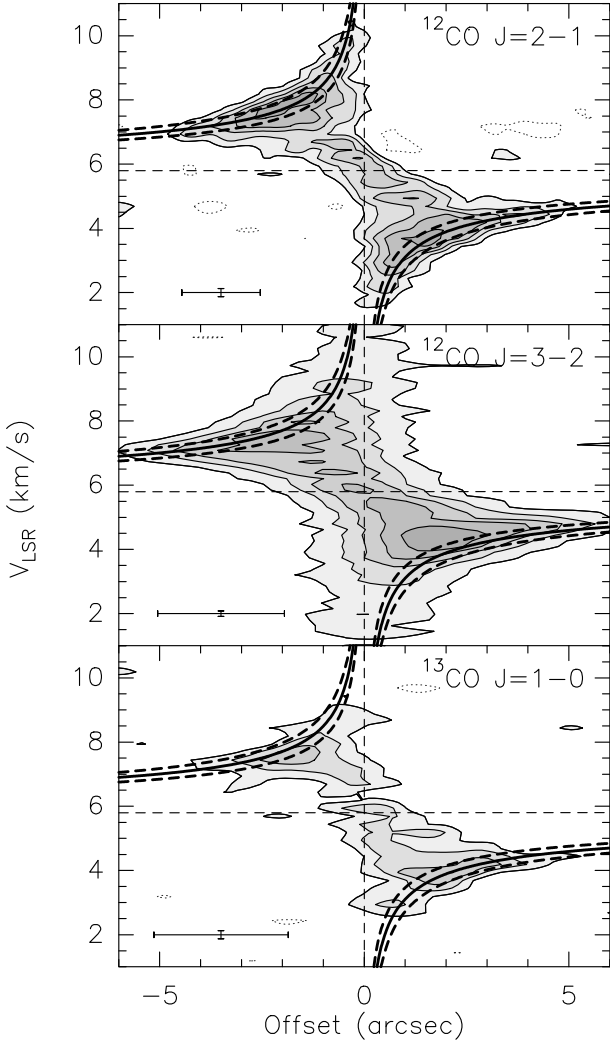


Fig. 5. Velocity-position plots along the plane of the disk for the ^{12}CO $J=2-1$ (upper panel), the ^{12}CO $J=3-2$ (middle panel) and the ^{13}CO $J=1-0$ (lower panel) transitions. The angular offset is measured with respect to the phase center of the observations corresponding to the position of the central star. The contour levels are spaced by 2σ corresponding to 0.14 Jy/beam, 1 Jy/beam and 0.06 Jy/beam respectively. The cross in the lower left of each panel gives the angular and spectral resolution of the corresponding map. The thick solid lines marks the border where emission is expected for a Keplerian disk inclined by 45° and rotating around a $2.0 M_\odot$ point source; the external and internal dashed lines correspond to stellar masses of $2.5 M_\odot$ and $1.5 M_\odot$ respectively. The horizontal and vertical straight dashed lines mark the systemic velocity (5.8 km/sec) and the position of the continuum peak.

brightness below the sensitivity limit. If we extend the disk model that fit the continuum to the outer radius of the CO, we predict a continuum emission between 200 AU and 550 AU which would be easily detected in our observations (see Fig. 9). A similar difference in the dust and gas

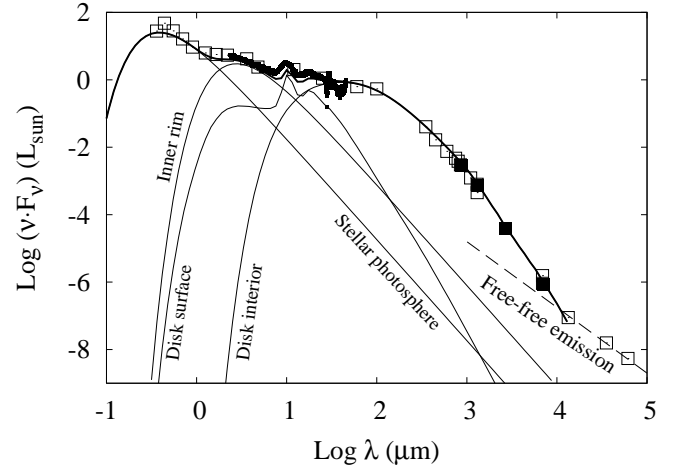


Fig. 6. HD 163296 spectral energy distribution. Data from literature are shown with empty squares (Mannings 1994; Natta et al. 2004; de Winter et al. 2001) and dots (ISO-SW). Our new measurements (see Tab.1) are shown with full squares. The observed fluxes at 3.6 cm and 6.1 cm have been used to calculate the free-free contribution (dashed line) to the observed flux assuming a free-free spectral index of 0.6. Free-free subtracted fluxes are shown at 7 mm while at shorter wavelength the free-free contribution is negligible. The solid line shows the prediction of our disk model as discussed in Sec. 5.2. The resulting spectral index α_{mm} between 0.87 and 7 mm ($F_\lambda \propto \lambda^{-\alpha_{mm}}$) is 3.0 ± 0.1 .

outer radii has been also reported by Piétu et al. (2005) for the Herbig Ae star AB Aur.

To reconcile CO and dust observations, it is necessary to introduce a sharp drop in the continuum emission of a factor > 30 at a radius of about 200 AU. With such a drop, the millimeter fluxes at larger r will be below the sensitivity of our observations and will be lost in the observational noise. What can be the origin of such a drop?

In the optically thin regime, which is appropriate for the outer regions of the disk, the continuum flux emitted at distance r from the star depends on the mass surface density $\Sigma(r)$, the dust/gas ratio $\Pi(r)$, the dust opacity $k_\nu(r)$ and the midplane dust temperature $T(r)$ through the relation

$$F_\nu(r) \propto \Sigma(r) \cdot \Pi(r) \cdot k_\nu(r) \cdot T(r). \quad (5)$$

It is possible that a different disk geometry (e.g., a lower flaring angle) gives a midplane dust temperature lower than the values predicted by our disk model. A lower temperature limit, of ~ 10 K, is however imposed by the equilibrium with the interstellar radiation field. Given that our fully flared disk model predicts temperatures of 20-30 K in the millimeter emitting regions, one can reduce F_ν by a factor 3 at most.

A second possibility to explain the observed flux depletion is that the dust opacity $k_\nu(r)$ at distance larger

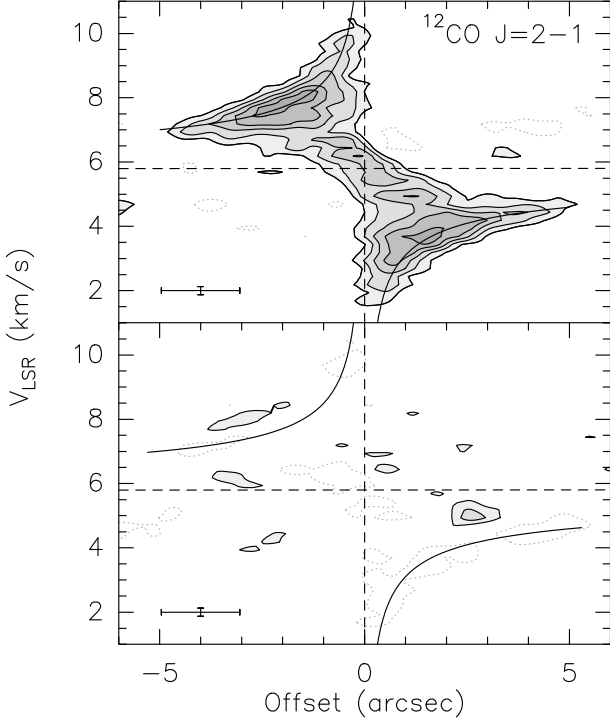


Fig. 8. Comparison between the observed and the model predicted ^{12}CO J=2–1 emission. The upper panel shows the position-velocity diagram for the ^{12}CO J=2–1 transition (as in Fig. 5). The lower panel shows the residuals relative to the best fit model parameters reported in Tab. 2. The contour levels are at 2σ as in Fig. 5.

than 200 AU is much lower because most of the grains have grown into very large bodies.

Finally, a third possibility is that the dust density, i.e. $\Sigma(r) \cdot \Pi(r)$, is in some way depleted at large distances. The values of the gas density $\Sigma(r)$ obtained by the CO lines analysis (see Tab. 2) induce however to exclude the existence of the strong discontinuity in the gas radial density profile required to explain a flux depletion factor > 30 since a drop of a factor ~ 10 in the ^{13}CO distribution at $r > 200$ AU will already produce small but observable effects on the line emission. On the other hand, it is possible that the ratio dust/gas $\Pi(r)$ decreases very rapidly in the outer disk either due to the formation and fast migration of meter size bodies or to the presence of planetesimals or planets which create a gap in the dust distribution. It is worth to note that the dynamical perturbation induced by such large bodies on the surrounding material (see the review of Papaloizou et al., 2007) may also account for the asymmetric dust density distribution detected in the continuum maps (Fig. 7).

The presence of a giant planet, or a brown dwarf, orbiting in the outer disk of HD 163296 has also been suggested by Grady et al. (2000), in order to explain the dark line observed in the scattered light HST images between 300 AU and 350 AU from the central star. While planets are invoked to explain the large inner gaps observed in the

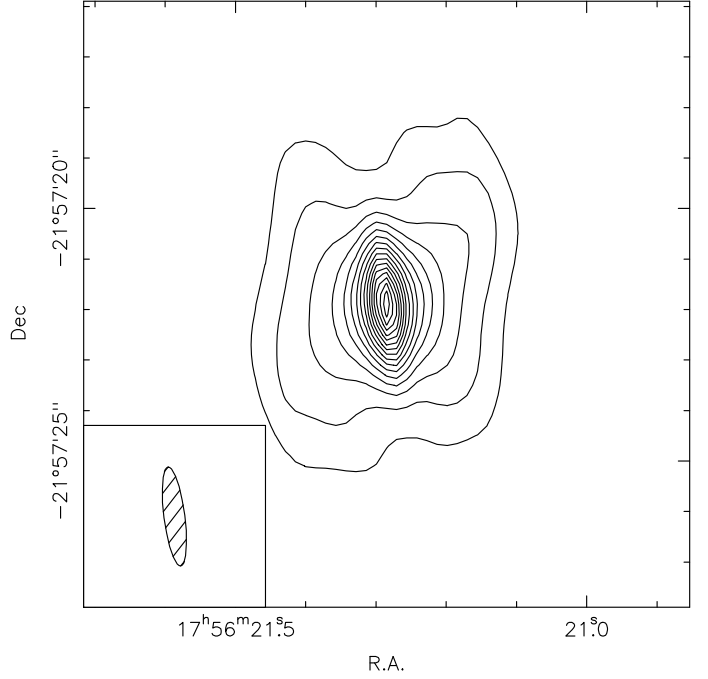


Fig. 9. Model predicted 1.3 mm continuum emission obtained extrapolating the dust surface density inferred inside the radius of 200 AU to the CO outer radius of 550 AU. The contours are spaced by 3σ corresponding to 0.12 mJy. See Fig. 1 for the comparison with the observations.

dust distribution in the so called “transitional disks” (i.e., Calvet et al., 2005), HD 163296 will be, if confirmed by future observations, the first case in which a sub-stellar mass companion is found in the outer disk of a pre-main sequence star.

6.4. Disk surface density and mass

Both the dust continuum emission and the CO lines indicate a rather shallow surface density profile, $\Sigma \propto r^{-0.8}$ corresponding to a gas + dust mass of $0.05 \pm 0.01 M_{\odot}$ if the disk outer radius is 200 AU. However, if, as we believe, the gaseous disk extends with the same surface density profile all way to 540 AU the inferred disk mass is much larger, $0.17 M_{\odot}$.

An additional uncertainty on the disk mass comes from the uncertainty on the dust opacity, as discussed in Natta et al. (2007). Although a disk mass of $0.17 M_{\odot}$ (6% M_{\star}) is probably a lower limit, the observed Keplerian rotation pattern indicates that the disk should not be much more massive. In this case one expects deviations from Keplerian rotation (Lodato and Bertin, 2003) as observed in massive disks (Cesaroni et al., 2005).

The example of HD 163296 illustrates how the simple disk mass derivation from the observed millimeter flux (see Sec 3.4) can be wrong for a variety of reasons, even when the emission is optically thin. In the case of HD 163296, only 30% of the total mass (i.e., the fraction inside 200 AU) contribute to the continuum millimeter flux. On the

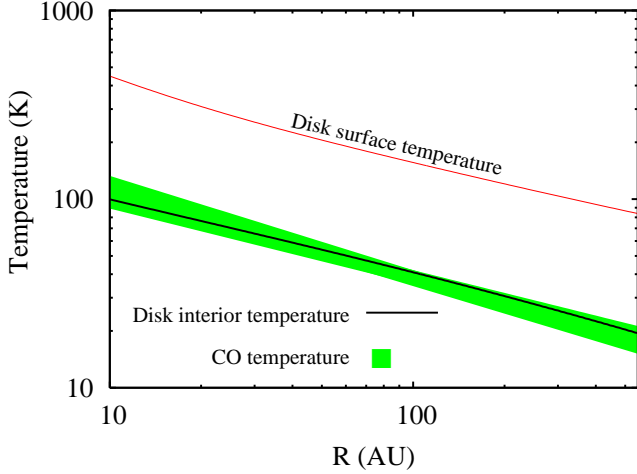


Fig. 10. Comparison between the dust and the CO temperature. As labelled in the figure, the thin-solid line corresponds to the dust temperature in the optically thin disk surface, while the thick solid line corresponds to the dust temperature in the disk interior. The CO temperature is indicated with the shaded region, taking into consideration the uncertainties. The model parameters are those reported in column 3 of Tab. 2

other hand, the disk is hotter than the 30 K assumed in Eq. 2. The two effects cancel in part so that the “simple” and “correct” values differ by about 50% (for the same $k_{1.3\text{mm}}$ normalization).

6.5. CO vs dust temperature

At the actual gas density both the ^{12}CO and ^{13}CO lines are optically thick and lead to similar CO excitation temperatures expressed by the relation $T(r) \sim 40\text{K} \cdot (r/100\text{AU})^{-0.5}$. Fig. 10 shows the comparison between this CO temperature (shaded region) and the dust temperature corresponding to the same disk model. The disk interior temperature T_i (thick-solid line) and the disk surface temperature T_s (thin-solid line), calculated using our two-layer disk model, correspond respectively to disk regions where $\tau_\star \gg 3$ and $\tau_\star \simeq 1$ (Dullemond et al. 2002); τ_\star is the optical depth for the stellar radiation calculated along the radial direction. The equivalence between the CO and the dust temperature can thus be interpreted as the evidence that the CO, and in particular the ^{12}CO , lines are emitted by the gas present at such values of the optical depth, e.g. well under the disk surface. Is this result compatible with the high optical depth of the ^{12}CO lines?

Assuming that H_2 and CO are well mixed all over the vertical extension of the disk and assuming also the standard ratio $^{12}\text{CO}/\text{H}_2 = 7.5 \cdot 10^{-5}$, the ^{12}CO lines should be emitted by disk regions well above the disk surface, defined as the height where $\tau_\star = 1$. In this situation, we expect a CO temperature close to the disk surface temperature, or even higher if the gas and the dust are decoupled

(Jonkheid et al., 2006). On the other hand CO molecules on the superficial layers of the disk are expected to be photo-dissociated by the UV photons emitted by the hot central star. In particular, for an Herbig Ae star similar to HD 163296, Jonkheid et al. (2006) show that the CO photo-dissociation occurs in the disk regions where the optical depth to the stellar UV radiation field is $\tau_{UV} \lesssim 3$ (see Fig 5.6 therein). Therefore, the CO and disk interior temperature are expected to be similar if $\tau_{UV} \lesssim \tau_\star$, i.e., if $k_{UV} \lesssim k_\star^P$, where k_\star^P is the dust opacity averaged on the stellar spectrum. We think that this is the case in HD 163296.

The dust opacity is a complex quantity that depends on the dust chemical composition, structure and on the grain size distribution. The condition $k_{UV} \lesssim k_\star^P$ is generally satisfied by large grains. In the case of HD 163296 one needs, for example, compact silicate grains larger than $0.1\mu\text{m}$ or porous grains of silicate and carbonaceous materials larger than few microns (see Fig. 11). Cooler stars require larger grains, unless significant UV excess is present.

If CO survives only in the disk interior, we expect that lines with different optical depth will have similar temperatures. On the contrary, if CO is present in the disk surface layers, lines with higher optical depth should have higher excitation temperatures.

The few existing observations indicate that all cases occur. Piétu et al. (2007) have recently reported that for the HAe stars MWC 480 and AB Aur and the TTS DM Tau, the ^{12}CO and ^{13}CO lines are characterized by different temperatures, while in the case of the TTS LkCa 15 the CO temperatures are all similar. We suggest that these differences are due to different dust properties (i.e. different composition, grain growth and settling) and stellar spectra.

6.6. CO isotopic abundances

The values of $\Sigma_{10\text{AU}}$ reported in Tab. 2 indicate that the ^{13}CO J=1–0 emission requires a ratio $^{13}\text{CO}/\text{H}_2 \sim 10^{-7}$, about a factor 10 lower than what found in interstellar clouds. From the non-detection of the C^{18}O J=1–0 line we estimate that the C^{18}O should be depleted of a factor > 60 with respect to the typical ratio $^{12}\text{CO}/\text{C}^{18}\text{O} = 550$. We note that a similar trend of depletion from ^{12}CO to ^{13}CO and C^{18}O has been found by Dutrey et al. (1994, 1996) in a number of TTS. On the other hand an over-abundance of ^{13}CO has been found in DM Tau, MWC 480 and LkCa 15 (Piétu et al. 2007) while for DM Tau, Dartois et al. (2003) find that all the CO isotopomers (^{12}CO , ^{13}CO and C^{18}O) are depleted by the same factor ~ 10 . The observational picture is still very uncertain and deserves further investigations.

In the case of HD 163296, the gas temperature always higher than 20 K rules out the condensation of CO onto dust grains as possible cause of the CO isotopomers depletion. Alternatively, Jonkheid et al. (2006) have recently pointed out that an higher ratio between the ^{12}CO and its

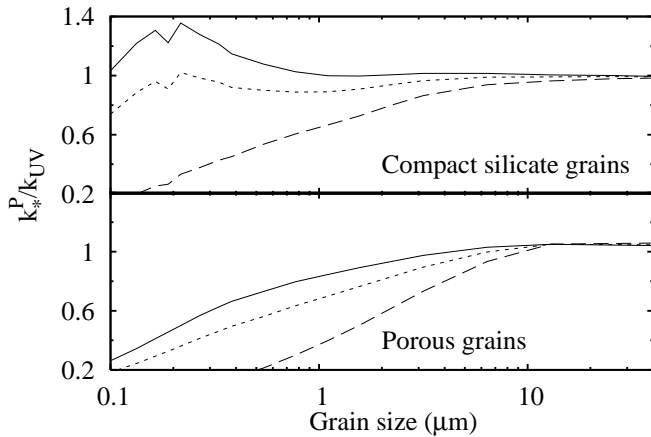


Fig. 11. Ratio between the Planck mean opacity at the stellar temperature k_*^P and the UV opacity k_{UV} for different grain sizes and composition. The upper panel shows the opacity ratio for compact silicate grains; the lower panel shows the ratio for porous grains composed by Olivine (17%), carbonates (53%) and vacuum (30%). The solid lines are relative to an H Ae star of $T_* = 10000\text{K}$, the long-dashed lines refer to a TTS with $T_* = 4000\text{ K}$ and the short-dashed lines to the same TTS with the addition of the UV excess radiation calculated so that $L_{UV}/L_* = 0.05$. This latter case is representative for the emission released by the gas accreting on the stellar surface.

isotopomers may be the consequence of grain growth and settling. This latter hypothesis is more convincing given the evidence of grain growth in the HD 163296 disk discussed in this work (see Sec. 5.2 and 6.5).

7. Summary

This paper presents new observations of the disk of HD 163296 in the dust continuum from 0.87 to 7 mm, ^{12}CO ($J=2-1$ and $J=3-2$) and ^{13}CO ($J=1-0$) lines. The disk is resolved in all lines and continuum.

We have compared the observations to the predictions of self-consistent disk models. We find that the disk, as seen in CO lines, is very large ($R = 540\text{ AU}$), with a Keplerian rotation pattern consistent with a central mass of 2.6 M_\odot . Within the observational errors, there is no evidence of non-Keplerian motions and/or significant turbulent broadening. We obtain a disk inclination of 46° , significantly lower than the value of $\sim 60^\circ$ found in literature.

The dust opacity has a power law dependence on wavelength $\kappa \propto \lambda^{-\beta}$ with $\beta = 1.0 \pm 0.1$ in the interval 0.87-7 mm. This value is similar to what has been measured in a number of spatially resolved disks of H Ae and TTS (e.g., Natta et al. 2004, Rodmann et al. 2006), and is very likely an indication that the bulk of the solid material in these disks has coagulated into very large bodies, of millimeter and centimeter size (Natta et al. 2007). Within the accu-

racy of our data we do not confirm the possible variation of β with r discussed in Natta et al. (2007).

The continuum observations constrain the surface density profile ($\Sigma \propto r^{0.8}$) for $r \leq 200\text{ AU}$. At larger radii, the continuum emission drops with respect to the model predictions by a factor 30 at least (at 1.3 mm). We argue that this may be due to the clearing of a very large gap by dynamical perturbations from a low mass companion or to the inward migration of the large bodies that may form in the outer disk.

The temperatures derived for CO lines of different optical depth are similar and equal to the dust temperature in the disk interior ($\tau_* \gg 1$). This requires that the dust opacity in the UV (which controls the CO dissociation) and in the wavelength range where the stellar radiation peaks are similar, as expected if grains have grown to micron size. Differences in the temperature of the CO lines can only be expected if CO is present in the disk surface layers. A variety of situation can occur depending on the exact dust composition and sizes and on the stellar radiation field.

A comparison of the disk properties derived from the dust continuum and the CO lines shows that the ^{13}CO $J=1-0$ emission is consistent with a ratio of $^{13}\text{CO}/\text{H}$ and $\text{C}^{18}\text{O}/\text{H}$ about a factor 10 and 60 lower than what is found in interstellar clouds.

8. Conclusions

The results discussed in this work can be interpreted as clues of the evolution occurring in the HD 163296 system. The presence of large grains in the disk midplane, the equivalence between the dust and CO temperature, the drop in the continuum dust emission further out 200 AU, its detected asymmetry and, maybe, the CO isotopomers depletion, all support the idea that the circumstellar disk is probably harboring the formation of large bodies, being in between a Class II pre-main sequence disk and an older debris disk.

On the other hand, it is important to underline that HD 163296 strongly differs from the so called *transitional disks* (Calvet et al., 2005) characterized by a clearing of the inner disk supposed to be originated by the presence of a giant planet. In the case of HD 163296 is indeed the outer disk that appear dust depleted. This conclusion opens a number of theoretical problem about how dust grains can growth in the low density outer disk environment. In this respect the recently improved PdB array, the new CARMA array and ALMA will bring in the next future to real observational breakthrough in the comprehension of circumstellar disk evolution and planetary formation.

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Appendix A: CO emission model

In order to analyze the CO emission we developed a numerical code that solve the general formulation of the radiation transfer equation along each direction between the observer and the emitting source. If s is the linear coordinate along the line of sight, increasing from the observer ($s \equiv 0$) towards the source, the observed emission in each direction is given by the relation

$$I_\nu = \int_0^\infty S_\nu(s) e^{-\tau_\nu(s)} K_\nu(s) ds, \quad (\text{A.1})$$

where the optical depth is defined in each point s through

$$\tau_\nu(s) = \int_0^s K_\nu(s') ds' \quad (\text{A.2})$$

and K_ν is the absorbing coefficient of the interstellar medium. Given the high gas densities in the pre-main sequence circumstellar disks, we can assume that all the CO levels corresponding to the rotational transitions under investigation are thermalized. In this case the source function can be approximated by the Planck function

$$S_\nu(s) = B_\nu(T_{CO}(s)) = \frac{2h\nu^3}{c^2} \frac{1}{\exp(h\nu/kT_{CO}(s)) - 1}, \quad (\text{A.3})$$

depending only on the local temperature of the gas T_{CO} (c , h and k are respectively the light speed, the Planck and Boltzman constant).

The absorbing coefficient of the circumstellar medium is due both to gaseous CO and dust: $K_\nu(s) = K_\nu^{CO}(s) + K_\nu^d(s)$. For the dust $K_\nu^d(s) = \rho(s) \cdot k_\nu$, where $\rho(s)$ is the local density of the circumstellar material (gas+dust) and k_ν is the dust absorbing coefficient for total mass unit given in Eq. 3. The CO absorbing coefficient is given by the relation

$$K_\nu^{CO}(s) = n_l(s) \cdot \sigma_\nu(s) \quad (\text{A.4})$$

where $n_l(s)$ is the total number of CO molecules at the lower level l of the transition and $\sigma_\nu(s)$ is the CO absorbing cross section.

Calling m_0 and χ_{CO} the mean molecular weight of the gas and the fraction of CO present in the gas respectively, the number of molecules $n_l(s)$ is given by the Boltzman equation

$$n_l(s) = \chi_{CO} \frac{\rho(s)}{m_0} \cdot \frac{g_l e^{-E_l/kT_{CO}(s)}}{Z(T_{CO}(s))}, \quad (\text{A.5})$$

where $g_l = 2l + 1$ is the statistical weight of the lower level l of the transition, $E_l = (1/2)l(l+1)kT_1$ is the level energy, T_1 is the temperature equivalent to the transition energy and $Z(T_{CO}(s))$ is the partition function at the gas temperature $T_{CO}(s)$. Following Beckwith and Sargent (1993, and references therein), the absorbing cross section $\sigma_\nu(s)$ can be expressed in term of the integrated cross section of the transition σ_0 through the relation

$$\sigma_\nu(s) = \sigma_0 \cdot \phi_\nu(s) \cdot (1 - e^{-h\nu/kT_{CO}(s)}), \quad (\text{A.6})$$

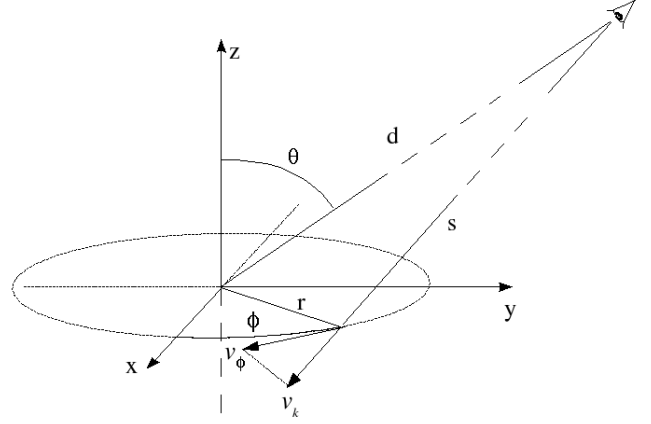


Fig. A.1. Schematic representation of the frame of reference adopted to calculate the CO emission arising from a rotating disk. The disk midplane and the observer lie respectively on the (x, y) and (y, z) planes; θ is the disk inclination; d is the distance between the observer and the central star; s is the linear coordinate along the line of sight increasing from the observer ($s \equiv 0$) towards the emitting source. Assuming that the material within the disk is subject to the Keplerian rotation around the central star, we call v_ϕ the velocity of a mass element at distance r and v_k the projection of v_ϕ along the line of sight.

where $\phi_\nu(s)$ is the intrinsic line profile

$$\phi_\nu(s) = \frac{c}{\nu_0} \cdot \frac{1}{\Delta V \sqrt{\pi}} \cdot \exp\left(-\frac{\Delta^2 v}{\Delta^2 V}\right), \quad (\text{A.7})$$

with

$$\Delta V = \sqrt{\frac{2kT_{CO}(s)}{m_{CO}} + v_{turb}^2} \quad (\text{A.8})$$

and

$$\sigma_0 = \frac{8\pi^3 k T_1}{h^2 c} \frac{(l+1)^2}{2l+1} \mu^2. \quad (\text{A.9})$$

In the previous equations, m_{CO} is the CO molecular weight, ν_0 is the rest frequency of the molecular transition, Δv is the difference between the velocity $v_{obs} = (c/\nu_0)(\nu - \nu_0)$, corresponding to the frequency ν , and the component of the gas velocity along the line of sight, $v_k(s)$, μ is the dipole moment of the CO molecule. Note that writing Eq. A.7, we assumed that the intrinsic line width depends both on the thermal velocity dispersion in the gas and on turbulent velocity v_{turb} .

As shown in Fig. 5 and described in Sec. 3.2, the observed velocity patterns in the CO transitions are in good agreement with the Keplerian rotation of the disk. We can thus assume that gas moves on circular orbits around the star characterized by a tangential velocity

$$v_\phi(r) = \sqrt{\frac{GM_\star}{r}}, \quad (\text{A.10})$$

where r is the radius of the orbit and M_\star is the stellar mass. To calculate the velocity $v_k(s)$, component of the tangential velocity $v_\phi(r)$ along the line of sight, it is useful to define a coordinates system centered on the star as shown in Fig. A.1: the (x, y) plane corresponds to the disk midplane; the observer lies in the (y, z) plane and its position it is defined by the inclination θ and the distance d from the star; each point of the circumstellar space can be defined through the cylindrical coordinates $r = \sqrt{x^2 + y^2}$, $\phi = \arctan(y/x)$ and z . Since $d \gg r$, we can write

$$v_k(s) \cong v_\phi(r) \cdot \cos \phi \cdot \sin \theta. \quad (\text{A.11})$$

Finally, the velocity $v_k(s)$ can be calculated for each direction, knowing the geometrical transformations between the coordinate s along the line of sight and the cylindrical coordinates r and ϕ .

In order to solve the described set of equations, we thus need an expression for the circumstellar mass density $\rho(s)$ and the temperature of the emitting gas $T_{CO}(s)$. In both cases we can assume the cylindrical symmetry and write $\rho(s) \equiv \rho(r, z)$ and $T_{CO}(s) \equiv T_{CO}(r)$.

For the emitting gas temperature, we choose the parameterization

$$T_{CO}(r) = T_{CO}(r_0)(r/r_0)^{-q}, \quad (\text{A.12})$$

while the mass density is calculated assuming that the disk is in hydrostatic equilibrium and vertically isothermal in the inner region at the midplane temperature $T_m(r)$, through the relation

$$\rho(r, z) = \rho_0(r) \cdot e^{-z^2/2h^2(r)}, \quad (\text{A.13})$$

valid between the disk inner and outer radii R_{in} and R_{out} . The density on the disk midplane $\rho_0(r)$ can be expressed as function of the surface mass density $\Sigma(r) = \Sigma_0(r/r_0)^{-p}$ through the relation

$$\rho_0(r) = \frac{\Sigma(r)}{\sqrt{2\pi}h(r)}. \quad (\text{A.14})$$

Finally, the pressure scale $h(r)$ is given by the relation

$$h(r) = \sqrt{\frac{2r^3 k T_i(r)}{GM_\star m_0}}, \quad (\text{A.15})$$

where $T_i(r)$ is obtained solving the structure of a stellar-irradiated passive disk as described in Dullemond et al. (2001).

Note that the emitting gas temperature T_{CO} has been parametrized independently of the disk interior temperature T_i , which governs the density structure of the disk. As pointed out by Dartois et al. (2003), the more optically thick CO transitions may be good tracer of the disk surface where the gas temperature is different from the disk interior.

The resulting model, produces brightness maps for each frequency (see Fig.A.2) that can be compared with the observations presented in Fig. 2 and 3.

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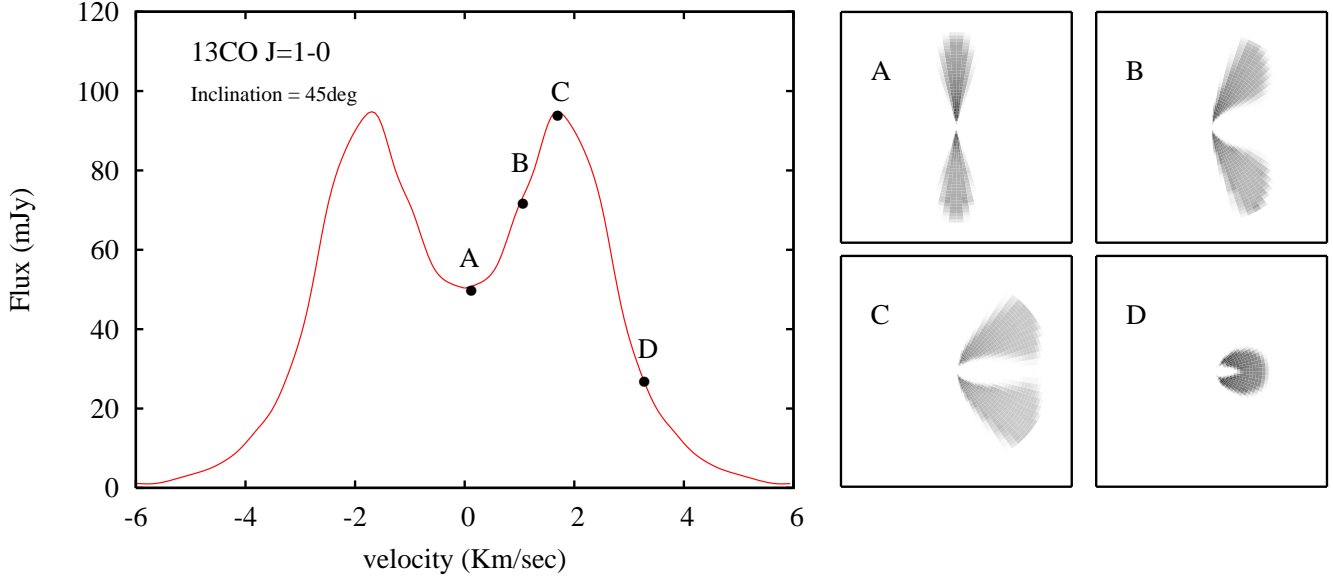


Fig. A.2. ^{13}CO J=1-0 simulated emission for a Keplerian disk inclined by 45° rotating around a central star of $1M_\odot$. The disk outer radius is $R_{out} = 100$ AU with a surface density $\Sigma(r) \propto r^{-1.5}$. The left panel show the spatial integrated line profile. The right panel shows the spatially resolved maps at different velocity as labelled in figure.

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